with $0.5 \%$ acetone in dichloromethane afforded $13.7 \mathrm{mg}(32 \%)$ of the desired dyad. The free amino group of the dyad was acetylated to yield 5 by simply dissolving the aminodyad in 2 mL of acetic anhydride and five drops of pyridine. The mixture was allowed to stand for 1 h . Following dilution with chloroform, extraction with a saturated solution of sodium bicarbonate, two extractions with water, and evaporation of the solvents at reduced pressure, the residue was purified by column chromatography on silica gel with chloroform to yield quantitatively diporphyrin 5: ${ }^{1} \mathrm{H}$ NMR ( $400 \mathrm{MHz}, \mathrm{CDCl}_{3}$ ) $\delta 8.85-9.01(16 \mathrm{H}, \mathrm{m}$, pyrrole-H), 8.49 ( $1 \mathrm{H}, \mathrm{s}, 5 \mathrm{Ar}-\mathrm{NH}$ ), $8.45(4 \mathrm{H}, \mathrm{AB}, J=8.2 \mathrm{~Hz}, 5 \mathrm{Ar} 2-\mathrm{H}$, $3-\mathrm{H}, 5-\mathrm{H}$ and $6-\mathrm{H}$ ), $8.33\left(2 \mathrm{H}, \mathrm{d}, J=8.4 \mathrm{~Hz}, 5^{\prime} \mathrm{Ar} 2-\mathrm{H}\right.$ and $6-\mathrm{H}$ ), 8.20 ( $2 \mathrm{H}, \mathrm{d}, J=8.4 \mathrm{~Hz}, 5^{\prime} \mathrm{Ar} 3-\mathrm{H}$ and $5-\mathrm{H}$ ), $8.17(2 \mathrm{H}, \mathrm{d}, J=8.2 \mathrm{~Hz}$, $15 \mathrm{Ar} 2-\mathrm{H}$ and $6-\mathrm{H}), 7.88(2 \mathrm{H}, \mathrm{d}, J=8.2 \mathrm{~Hz}, 15 \mathrm{Ar} 3-\mathrm{H}$ and $5-\mathrm{H}), 8.11$ $(4 \mathrm{H}, \mathrm{d}, J=7.9 \mathrm{~Hz}, 10,20 \mathrm{Ar} 2-\mathrm{H}$ and $6-\mathrm{H}), 7.57(4 \mathrm{H}, \mathrm{d}, J=7.9 \mathrm{~Hz}$, 10,20Ar3-H and 5-H), 7.46 ( $1 \mathrm{H}, \mathrm{s}, 15 \mathrm{Ar}-\mathrm{NH}$ ), 2.72 ( $6 \mathrm{H}, \mathrm{s}, \mathrm{Ar}-\mathrm{CH}_{3}$ ), 2.35 ( $3 \mathrm{H}, \mathrm{s}, \mathrm{COCH}_{3}$ ), -2.72 ( $2 \mathrm{H}, \mathrm{s}, \mathrm{NH}^{\prime}$ ), -2.81 ( $2 \mathrm{H}, \mathrm{s}, \mathrm{NH}$ ); UV-vis absorption (dichloromethane) $\lambda_{\max }(\mathrm{nm}) 420,512,554,590,650$; fluorescence emission ( $\lambda_{\mathrm{ex}}=590 \mathrm{~nm}$ in dichloromethane) $\lambda_{\text {max }}(\mathrm{nm}) 655$, 718.

Diporphyrin 6. Freshly prepared acid chloride 18 (from 30 mg ( 0.032 mmol ) of the acid) was dissolved in 10 mL of toluene, and the resulting solution was added to $8.0 \mathrm{mg}(0.012 \mathrm{mmol})$ of 19 dissolved in a mixture of toluene ( 2 mL ) and pyridine ( 0.5 mL ). The mixture was stirred for 5 h , and the solvent was then distilled at reduced pressure. The residue was dissolved in water and dichloromethane and extracted with dichloromethane. The organic layer was evaporated to dryness, the residue dissolved in toluene, and the resulting solution distilled to remove any residual water and pyridine. The residue was purified by chromatography on silica gel (dichloromethane) and recrystallization from dichloromethane and methanol to give 18 mg of compound 6 ( $95 \%$ yield): ${ }^{1} \mathrm{H}$ NMR ( $400 \mathrm{MHz}, \mathrm{CDCl}_{3}$ ) $\delta 8.88-9.01(16 \mathrm{H}, \mathrm{m}$, pyrrole-H), $8.50(1 \mathrm{H}$, $\mathrm{s}, 5 \mathrm{Ar}-\mathrm{NH}), 8.46(2 \mathrm{H}, \mathrm{AB}, J=9.0 \mathrm{~Hz}, 5 \mathrm{Ar} 3-\mathrm{H}$, and $5-\mathrm{H}), 8.47(2 \mathrm{H}$, AB $J=9.0 \mathrm{~Hz}, 5 \mathrm{Ar} 2-\mathrm{H}$ and $6-\mathrm{H}), 8.34\left(2 \mathrm{H}, \mathrm{d}, J=8.4 \mathrm{~Hz}, 5^{\prime} \mathrm{Ar}^{3}-\mathrm{H}\right.$ and $5-\mathrm{H}), 8.22\left(2 \mathrm{H}, \mathrm{d}, J=8.4 \mathrm{~Hz}, 5^{\prime} \mathrm{Ar} 2-\mathrm{H}\right.$ and $\left.6-\mathrm{H}\right), 8.13(4 \mathrm{H}, \mathrm{d}$, $J=7.6 \mathrm{~Hz}, 10,20 \mathrm{Ar} 2-\mathrm{H}$ and $6-\mathrm{H}), 8.11(2 \mathrm{H}, \mathrm{d}, J=7.0 \mathrm{~Hz}, 15 \mathrm{Ar} 2-\mathrm{H}$ and $6-\mathrm{H}), 7.58(4 \mathrm{H}, \mathrm{d}, J=7.6 \mathrm{~Hz}, 10,20 \mathrm{Ar} 3-\mathrm{H}$ and $5-\mathrm{H}), 7.56(2 \mathrm{H}$, $\mathrm{d}, J=7.0 \mathrm{~Hz}, 15 \mathrm{Ar} 3-\mathrm{H}$ and $5-\mathrm{H}), 2.72\left(6 \mathrm{H}, \mathrm{s}, 10,20 \mathrm{Ar}-\mathrm{CH}_{3}\right), 2.71$ ( 3 $\mathrm{H}, \mathrm{s}, 10,15,20 \mathrm{Ar}-\mathrm{CH}_{3}$ ), -2.87 ( $2 \mathrm{H}, \mathrm{s}$, pyrrole-NH), $-2.78(2 \mathrm{H}, \mathrm{s}, \mathrm{PF} 15$ pyrrole-NH); UV-vis absorption (dichloromethane) $\lambda_{\max }(\mathrm{nm}), 420,514$,

552, 590, 648; fluorescence emission ( $\lambda_{\mathrm{ex}}=590 \mathrm{~nm}$, dichloromethane) $\lambda_{\text {max }}(\mathrm{nm}), 652,718$.
Zinc 5-(4-Aminophenyl)-10,15,20-tris(4-methylphenyl)porphyrin (20) was prepared from $15 \mathrm{mg}(0.022 \mathrm{mmol})$ of 19 via the method described for 10. The yield was 14 mg ( $86 \%$ ): UV-vis absorption (dichloromethane) $\lambda_{\max }(\mathrm{nm}) 422,550,590$; fluorescence emission ( $\lambda_{\mathrm{ex}}=550 \mathrm{~nm}$ in dichloromethane) $\lambda_{\max }(\mathrm{nm}) 603,649$.

Diporphyrin 7. Freshly prepared acid chloride 18 (from 20 mg ( 0.022 mmol ) of the acid) was dissolved in 10 mL of toluene, and the resulting solution was added to $7.4 \mathrm{mg}(0.010 \mathrm{mmol})$ of 20 dissolved in a mixture of toluene ( 2 mL ) and pyridine ( 2 mL ). The mixture was stirred for 14 $h$, and the solvents were then evaporated at reduced pressure. The residue was dissolved in dichloromethane and extracted with water. The organic layer was evaporated to dryness, the residue dissolved in toluene, and the resulting solution distilled to remove any residual water and pyridine. The residue was purified by chromatography on silica gel (dichloromethane) and recrystallization from dichloromethane and methanol to give 9.0 mg of 7 ( $54 \%$ yield): ${ }^{1} \mathrm{H}$ NMR ( $400 \mathrm{MHz}, \mathrm{CDCl}_{3}$ ) $\delta 8.95-9.02(16 \mathrm{H}, \mathrm{m}$, pyrrole-H), $8.50(1 \mathrm{H}, \mathrm{s}, 5 \mathrm{Ar}-\mathrm{NH}), 8.46(2 \mathrm{H}$, $\mathrm{AB}, J=9.0 \mathrm{~Hz}, 5 \mathrm{Ar} 3-\mathrm{H}$, and $5-\mathrm{H}), 8.47(2 \mathrm{H}, \mathrm{AB}, J=9.0 \mathrm{~Hz}, 5 \mathrm{Ar} 2-\mathrm{H}$ and $6-\mathrm{H}), 8.34\left(2 \mathrm{H}, \mathrm{d}, J=8.4 \mathrm{~Hz}, 5^{\prime} \mathrm{Ar} 3-\mathrm{H}\right.$ and $\left.5-\mathrm{H}\right), 8.22(2 \mathrm{H}, \mathrm{d}$, $J=8.4 \mathrm{~Hz}, 5^{\prime} \mathrm{Ar} 2-\mathrm{H}$ and $\left.6-\mathrm{H}\right), 8.13(4 \mathrm{H}, \mathrm{d}, J=7.6 \mathrm{~Hz}, 10,20 \mathrm{Ar} 2-\mathrm{H}$ and $6-\mathrm{H}), 8.11(2 \mathrm{H}, \mathrm{d}, J=7.0 \mathrm{~Hz}, 15 \mathrm{Ar} 2-\mathrm{H}$ and $6-\mathrm{H}), 7.58(4 \mathrm{H}, \mathrm{d}$, $J=7.6 \mathrm{~Hz}, 10,20 \mathrm{Ar} 3 \cdot \mathrm{H}$ and $5-\mathrm{H}), 7.56(2 \mathrm{H}, \mathrm{d}, J=7.0 \mathrm{~Hz}, 15 \mathrm{Ar} 3-\mathrm{H}$ and $5-\mathrm{H}$ ), $2.72\left(6 \mathrm{H}, \mathrm{s}, 10,20 \mathrm{Ar}-\mathrm{CH}_{3}\right), 2.71\left(3 \mathrm{H}, \mathrm{s}, 15 \mathrm{Ar}-\mathrm{CH}_{3}\right),-2.78$ ( $2 \mathrm{H}, \mathrm{s}, \mathrm{PF} 15$ pyrrole-NH); UV-vis absorption (dichloromethane) $\lambda_{\text {max }}$ (nm), 422, 510, 550, 588, 640; fluorescence emission ( $\lambda_{\mathrm{ex}}=550 \mathrm{~nm}$, dichloromethane) $\lambda_{\max }(\mathrm{nm}), 600,643,710$.

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# Tetramethylene Dications $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ : Are the Norbornadiene Dication, the Pagodane Dication, and Related Systems Aromatic?" 

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#### Abstract

The $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ potential energy hypersurface has been investigated by semiempirical and ab initio calculations. The global minimum is an acyclic structure of $C_{i}$ symmetry. Harmonic vibrational analysis of the rectangular cyclobutane dication $\left(D_{2 h}\right)$, which serves as a model for " $\sigma$-aromatic" pagodane and norbornadiene dications, indicates three imaginary frequencies. Nonetheless, strong evidence that the pagodane dication has a nonclassical, "aromatic" structure of $D_{2 h}$ symmetry is presented. A rapid equilibrium of two classical $C_{2 v}$ structures and a diradical $D_{2 h}$ species, in which both are consistent with the experimental NMR spectroscopic data, can be excluded on the basis of our theoretical investigations. The norbornadiene dication is also predicted to be stabilized by aromaticity, whereas structures with larger distances between the two formal ethylene radical cations are predicted to exhibit increasing diradicaloid character.


Treated at $-80^{\circ} \mathrm{C}$ with $\mathrm{SbF}_{5} / \mathrm{SO}_{2} \mathrm{ClF}$, [1.1.1.1]pagodane (1) is oxidized to give a dication persistent for several hours at room temperature. ${ }^{1}$ This behavior is remarkable since no stabilizing aromatic or heteroatomic substituents are present. ${ }^{13} \mathrm{C}$ and ${ }^{1} \mathrm{H}$

[^0]NMR spectra indicate the preservation of the original $D_{2 h}$ symmetry at least on the observational time scale. Quenching 1 with methanol yields the decacyclic derivative 2. The remarkable stability of the dication implies an extraordinary electronic

[^1]

Figure 1. Corresponding orbitals of the cyclobutane and the cyclobutadiene dications. These are represented in idealized rectangular ( $D_{2 h}$ ) and square ( $D_{4 k}$ ) symmetries, even though other forms are more stable. ${ }^{21 a}$
structure. To account for the experimental facts, a $\sigma$-aromatic formulation 4, rather than a set of equilibrating classical species 5 , was proposed. ${ }^{1.2}$


4
$\sigma$-aromaic
$\mathrm{D}_{2 \mathrm{r}}$

$\xrightarrow{\mathbf{S b F} / \mathrm{SO}_{2} \mathrm{ClF}}$



5
classical structure
$\mathrm{C}_{2 v}$


2


6
singlet diradical dication
$\mathrm{D}_{\text {2h }}$

In the present context, " $\sigma$-aromatic" implies significant overlap between the orbitals on the more distant carbons of 4. This is illustrated in Figure 1 for the parent system, the cyclobutane dication. The orbitals shown are topologically equivalent to those for the cyclobutadiene dications. In both cases, formal interactions between two olefin radical cation moieties are involved. If the separation is large, as in 6 , no significant stabilization due to such interactions can be expected.
MNDO calculations indicated both the $D_{2 h}$ structure 4 and the $C_{2 v}$ structure 5 to be minima on the energy hypersurface, the "aromatic" structure being $4 \mathrm{kcal} / \mathrm{mol}$ more stable than its classical counterpart. ${ }^{2}$ These theoretical results have been interpreted as a further support for the $D_{2 h}$ structure. ${ }^{2}$ Although the available evidence seems to favor the aromatic structure 4 , neither a fast equilibrium of classical $C_{20}$ structures 5 nor a singlet diradical dication 6 can be excluded. Indeed, the MNDO geometry of 4 would be consistent with the latter. The longer bond distance in the central four-membered ring in 4 was calculated to be 2.592 $\AA$. Through space interactions over such a distance should be extremely weak, the contraction of the radial extension of the orbitals caused by the positive charge should further weaken the interaction between the two formal ethylene radical cation units. The pagodane dication is not the first dication for which a $\sigma$ aromatic structure was proposed. In 1981, Hogeveen and coworkers ${ }^{3}$ synthesized the octamethylnorbornadiene dication via ionization and rearrangement of a tricyclic alcohol. On the basis of their NMR and quenching results, they proposed the structure 7.

Dication 7 is stable up to $-40^{\circ} \mathrm{C}$ in magic acid solution. The appearance of only one signal in the ${ }^{1} \mathrm{H}$ NMR spectrum ( $\delta 2.47$ )

[^2]
and only two ${ }^{13} \mathrm{C}$ signals ( $\delta 151.7$, singlet, and $\delta 16.9$, quartet) even at low temperatures was explained by fast methyl and skeleton carbon scramblings.
While the geometries, electronic structures, and the stabilities ("aromaticity") of these pagodane (4) and norbornadiene (7) dications are intriguing problems themselves, they are part of a more general picture.
Tetramethylene dications $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ and their derivatives are of interest in other contexts as well. In his Noble Prize lecture, Building Bridges Between Inorganic and Organic Chemistry, R . Hoffmann described numerous isolobal analogies, ${ }^{4}$ e.g.


He then extended the same reasoning; "It is interesting to speculate when we might see the missing members of the series on the organic side, $(\mathrm{CO})_{4} \mathrm{Re}\left(\mathrm{CH}_{3}\right)_{3}$ and $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+\eta}$. Implied is structure 9 (Figure 2) for the cyclobutane dication. Hoffmann's cyclic $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ structure 9 seems peculiar at first sight because of the "extra" transannular bond. At the time of Hoffmann's address, we had already been concerned with the question of what happens structurally when two electrons are removed from a saturated hydrocarbon. For example, in one of the states of triplet $\mathrm{C}_{2} \mathrm{H}_{6}{ }^{2+}$, extra $\mathrm{C}-\mathrm{C}$ bonding results when two valence electrons are removed from the degenerate higher lying orbitals with $\mathrm{C}-\mathrm{C}$ antibonding character. ${ }^{5}$ Structure 9 can be understood similarly. The cyclobutane HOMO's are a doubly degenerate set of Walsh-type orbitals of $\pi^{*}$-symmetry:


If two electrons are lost from one of these orbitals to give a singlet cyclobutane dication, one of the repulsive transannular interactions should be relieved and the distortion implied by structure 9 should result. Alternatively, the rhombic structure 9 could be viewed as a transition state for a possible dyotropic rearrangement ${ }^{6}$ of an open dication 8 .
Similar doubly bridged arrangements have been found in dilithioacetylene, ${ }^{66}$ dilithioethylene, ${ }^{7}$ and dilithioethane. ${ }^{8}$


## Computational Methods

Semiempirical calculations (MINDO/3, MNDO, AM1) were performed with the AMPAC program package ${ }^{9}$ and $a b$ initio calculations of

[^3]




$12 c_{2 v}$

Figure 2. Geometries of five different $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ structures optimized at the MP2/6-31 $\mathrm{G}^{*}$ level (6-31 $\mathrm{G}^{*}$ geometries in parentheses).
Table I. Relative Energies of $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ Structures ${ }^{a}$

| compd | MNDO | $\begin{gathered} 3-21 G / / \\ 3-21 G \end{gathered}$ | $\begin{gathered} 6-31 \mathrm{G}^{*} / / \\ 6-31 \mathrm{G}^{*} \end{gathered}$ | $\begin{gathered} \mathrm{MP2} / \\ 6-31 \mathrm{G}^{*} / / \\ 6-31 \mathrm{G}^{*} \end{gathered}$ | $\begin{gathered} \text { MP2/ } \\ 6-31 G^{*} / / \\ \text { MP2FULL/ } \\ 6-31 G^{*} \end{gathered}$ | $\begin{gathered} \text { MP3/ } \\ 6-31 G^{*} / / \\ \text { MP2FULL/ } \\ 6-31 G^{*} \end{gathered}$ | $\begin{gathered} \text { MP4SDTQ/ } \\ \text { 6-31G*// } \\ \text { MP2FULL/ } \\ 6-31 G^{*} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $8\left(C_{i}\right)$ | 0.0 | 0.0 (0) | 0.0 (0) | 0.0 | 0.0 (0) | 0.0 | 0.0 |
| $9\left(D_{2 h}\right)$ | 75.6 | 60.9 (1) | 53.5 (1) | 14.9 | 15.4 (2) | 25.8 | 31.9 |
| $10\left(D_{2 d}\right)$ | 76.5 | 34.6 (3) | 37.0 (3) | 25.8 | 26.2 (3) | 29.2 | 37.1 |
| $11\left(D_{2 h}\right)$ | 66.2 | 28.8 (3) | 34.4 (3) | 22.1 | 22.2 (2) | 25.8 | 33.7 |
| $12\left(C_{2 v}\right)$ | 19.7 | 25.5 (3) | 24.1 (3) | 25.3 | $b$ | $b$ | $b$ |

${ }^{a}$ Energies in kilocalories per mole. The number of imaginary frequencies is given in parentheses. ${ }^{b}$ Gives 11 ; see text.
the $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ structures with the GAUSSIANB8 ${ }^{10}$ package using the standard basis sets and post SCF treatments. ${ }^{11}$ The pagodane dications 4 and 5 the norbornadienyl dication 13, and the tricyclic dications 14 and 15 were optimized with CADPAC. ${ }^{12}$ Harmonic vibration frequency modes were calculated with the analytic gradient methods implemented in CADPAC. MC-SCF calculations were performed with the GAMESS program. ${ }^{13}$ Reference states were selected according to the CI eigenvector of a MNDO full Cl calculation using all states with coefficients greater than $0.025 .{ }^{13} \mathrm{C}$-shift calculations were computed with IGLO ${ }^{14}$ with double-ร (DZ) basis sets.

## Energy and Structure of $\left(\mathrm{CH}_{2}\right)_{4}{ }^{\mathbf{2 +}}$ Isomers

Tetramethylene cations $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ can be viewed as model compounds of pagodane and norbornadienyl dication as well as those of the rhombic structure 9 and its isolobal analogues. In order to gain further insight in the electronic structures and relative stabilities, we carried out extensive investigations of the $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ potential energy hypersurface at semiempirical and lower ab initio
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Figure 3. Relative energies of five different $\left(\mathrm{CH}_{2}\right)_{4}{ }^{2+}$ structures at various levels of theory. The values are based on the global minimum of $C_{i}$ symmetry.
levels. Five species were selected as being of primary interest, and the geometries were reoptimized at MP2 (FULL) $/ 6-31 \mathrm{G}^{*}$, i.e., including correlation corrections of the second order of perturbation theory on a split valence basis set augmented by polarization functions on carbon (Figure 3). Structures 5, 8, and 12 are representatives of open 1,4-butadiyl dications; 9 and 11 are the two $D_{2 h}$ dications expected from removal of two electrons from cyclobutane. Alternatively, 9 can be viewed as the possible dyotropic rearrangement transition state of 8 and 11 as a complex between two ethylene radical cations. Another possible combi-

Table II. Energies ${ }^{\text {a }} \mathbf{4}$ and 5 , Calculated with MINDO/3, MNDO, AM1 and ab Initio 3-21G//3-21G, and MP2/3-21G//3-21G

|  | $\begin{gathered} \text { MINDO } / 3 \\ \Delta H_{\mathrm{f}}(\mathrm{kcal} / \mathrm{mol}) \end{gathered}$ | MNDO <br> $\Delta H f(\mathrm{kcal} / \mathrm{mol})$ | AM1 <br> $\Delta H_{\mathrm{f}}(\mathrm{kcal} / \mathrm{mol})$ | $\begin{gathered} 3-21 G / / 3-21 G \\ \text { hartree/particle } \end{gathered}$ | $\begin{gathered} \mathrm{MP} 2 / 3-21 \mathrm{G} / / \\ 3-21 \mathrm{G} \\ \text { hartree/particle } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 4 D_{2 h} \\ & 5 C_{2 v} \end{aligned}$ | $\begin{aligned} & 617.27 \\ & b \end{aligned}$ | $\begin{aligned} & 559.51 \\ & 563.54 \end{aligned}$ | $\begin{aligned} & 523.69 \\ & b \end{aligned}$ | $\begin{aligned} & -764.1552 \\ & b \end{aligned}$ | -765.7838 |

${ }^{a}$ All stationary points were confirmed to be minima by harmonic frequency analysis. ${ }^{b}$ Closes to rectangular structure 4 upon optimization.


Figure 4. Frequency modes of $11 ; \mathrm{MP2} / 6-31 \mathrm{G}^{*}$ optimized structure ( $6-31 \mathrm{G}^{*}$ values in parentheses). Only modes of carbon atoms are shown.
nation of the latter has $D_{2 h}$ symmetry 10 .
With optimization at the split valence (3-21G), polarized (6$31 \mathrm{G}^{*}$ ), and correlated (MP2/6-31G*) ab initio levels, the open form 8 with $C_{l}$ symmetry is the only minimum (Table I). Both terminal $\mathrm{CH}_{2}$ groups are twisted $12.5^{\circ}$ relative to the plane formed by the carbon atoms. However, at the $6-31 \mathrm{G}^{*} / / 6-31 \mathrm{G}^{*}$ level the $C_{1}$-structure is only $0.1 \mathrm{kcal} / \mathrm{mol}$ lower in energy than the planar trans $C_{2 h}$ structure. Structures 11 ( $D_{2 h}, \sigma$-aromatic dication) and 12 ( $C_{2 v}$, classical dication) are interesting as models for the pagodane and norbornadiene dications. At the SCF level, 12 is more stable than its " $\sigma$-aromatic" counterpart 11, but both have three imaginary frequencies. ${ }^{15}$ One of these, mode b of 11 (Figure 4), corresponds to the ring-opening motion toward 12. At the MP2-correlated level, this frequency mode disappears and 11 becomes more stable than 12. Optimizing the classical structure 12 at MP2/6-31G* within the $C_{2 v}$ point group leads to ring closure to 11. The two imaginary frequencies a and c remain in 11 at the MP2 level. Frequency mode a describes a distortion toward the rhombic structure 9 , while the out of plane motion c corresponds to a distortion toward the $D_{2 d}$ structure 10. However, the latter has three imaginary frequencies and both 9 and 11 have two. Hence, besides 8, none of the other forms investigated are even true transition states.
Figure 3, which presents the relative energies at the various theoretical levels, shows that electron correlation is of critical importance for a proper description of structure 9 as well. Improvement of the basis set does not have a large effect on the relative energies of 9,10 , and 11 , but upon including the MP2 single-point energy, 9 becomes $38.6 \mathrm{kcal} / \mathrm{mol}$ more stable relative to the global minimum 8 and thus more stable than 11 and 10 At the MP2-optimized level, a second imaginary frequency appears. Thus, 9 is not the transition state of a dyotropic rearrangement as suggested previously, but a stationary point of higher order. The relative order of energies remains constant at the MP2-optimized level and at higher level of correlation (MP3 and MP4SDTQ)

The implications for the pagodane dication on the basis of these model results are obvious. The instability of the classical structure 12 toward the nonclassical 11 ( $D_{2 h}$ structure) should be even more pronounced in the case of the pagodane dication, where the system is constrained by a molecular framework of $D_{2 h}$ symmetry. This is demonstrated clearly by calculations of the pagodanes 4 and 5 with semiempirical and ab initio methods on the 3-21G//3-21G level (Tables II and III). Only with MNDO a minimum structure within the $C_{2 v}$ point group was found, which is $4.03 \mathrm{kcal} / \mathrm{mol}$ less stable than the $D_{2 h}$ structure. Optimizing 5 with MINDO/3 and AM1 as well as $3-21 \mathrm{G}$ leads to ring closure to $4 .{ }^{2}$ No energy minimum was found within the $C_{2 v}$ point group using these methods. These theoretical results provide good reasons for excluding the set of rapidly equilibrating classical structures 5

[^4]Table III. Selected Geometrical Parameters of 4 and 5, Calculated with MINDO/3, MNDO, AM1, and ab Initio 3-21G//3-21G

$4 D_{2 h}$

$5 \mathrm{C}_{2 \mathrm{v}}$

|  | $\mathbf{4}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | ---: |
| parameter $^{a}$ | MINDO/3 | MNDO | AMI | $3-21 G / /$ <br> $3-21 G$ | 5 <br> MNDO $^{6}$ |
| $1-2$ | 2.768 | 2.592 | 2.429 | 2.165 | 2.518 |
| $3-4$ | 2.768 | 2.592 | 2.429 | 2.165 | 1.723 |
| $2-3$ | 1.479 | 1.461 | 1.449 | 1.421 | 1.512 |
| $1-5$ | 1.524 | 1.511 | 1.488 | 1.513 | 1.514 |
| $3-7$ | 1.524 | 1.511 | 1.488 | 1.513 | 1.559 |
| $1-2-6$ | 83.5 | 86.5 | 88.8 | 93.1 | 88.4 |
| $4-3-7$ | 83.5 | 86.5 | 88.8 | 93.1 | 100.7 |
| $2-3-7$ | 111.1 | 111.6 | 111.1 | 111.4 | 107.9 |
| $3-2-6$ | 111.1 | 111.6 | 111.1 | 111.4 | 109.6 |

${ }^{a}$ Bond lengths in angstroms and angles in degrees. ${ }^{b}$ No MINDO/3, AM1, and 3-21G//3-21G data are given, since no minimum in $C_{2 v}$ could be found with these methods.


Figure 5. Correlation diagram; cycloaddition of two ethylene radical cations.

However, the singlet diradical cation still remains as a possible alternative to the proposed aromatic species.

## Diradical Character of the Pagodane Dication and Related Systems

The pagodane dication 4 can be viewed as a frozen aromatic transition state ${ }^{16 \mathrm{arc}}$ of the symmetry-allowed cycloaddition of two

[^5]

Figure 6. Energy splitting between the lowest singlet and triplet state of the cyclobutane dication system as a function of the reaction coordinate r. $\Delta E_{\mathrm{S}-\mathrm{T}}$ was calculated with MNDO full Cl and imposed $D_{2 h}$ symmetry.
spin-paired ethylene radical cations (Figure 5).
At large distances between the two ethylene radical cation units, the bonding $a_{1}$ and the antibonding $b_{2}$ MO's are degenerate, and according to Hund's rule, the system should be a perfect diradical. As the distance decreases (within the $D_{2 h}$ point group), the energy of the $b_{2}$ orbital rises because of its increasing antibonding character and $b_{1}$ is stabilized due to the increase in bonding along the reaction coordinate. The $b_{1}$ and $b_{2}$ levels cross. But since we are dealing with a dication, only the totally symmetric and bonding $a_{1}$ orbital is occupied. According to our calculations, this situation is realized in the parent aromatic dication 11. At this geometry and at all levels of ab initio theory including MNDO, the unoccupied $b_{1}$ and $b_{2}$ orbitals are almost degenerate. Where does the pagodane dication lie on this reaction coordinate? A bond length of more than $2.5 \AA$, as predicted by the MNDO calculations, should lead to considerable diradical character. There is a continuum from almost pure closed shell to a diradical nature depending on this geometric parameter. One cannot set a dividing line to clearly distinguish between closed shell and diradical but an indication for a diradicaloid character of a species can be derived from the energy splitting between its lowest singlet and triplet state ${ }^{17}$ (Figure 6).

Two ethylene radical cations at an infinite distance involve two degenerate noninteracting and singly occupied MO's. Thus, singlet and triplet states have the same energy and the system is a perfect diradical. Moving to the "transition state" increases the splitting. According to a MNDO full CI calculation, the singlet-triplet splitting in the aromatic dication 11 reaches a maximum value on the reaction coordinate, with $59 \mathrm{kcal} / \mathrm{mol}$ indicating a quite pure closed shell state. Shortening the distance even further leads eventually to the square dication, which is again a triplet diradical. Figure 6 shows the singlet-triplet splitting as a function of the bond length $r$ between the two formal ethylene radical cation units. Another sign for the "extent" of biradical character can be derived from the contribution of higher configurations to the overall wavefunction. Calculations along the reaction coordinate were performed with MNDO and full CI (Figure 7).

Like the singlet-triplet splitting result, these calculations again predict the geometry corresponding to 11 with $r=2.2 \AA$ to have the lowest diradicaloid character along the reaction coordinate. Three configurations account for more than $99.8 \%$ of the wavefunction of 11. This wavefunction $\psi$ can be expressed as a linear combination of the $\mathrm{a}_{1}{ }^{2}$ ground state and the two higher configurations $b_{1}{ }^{2}$ and $b_{2}{ }^{2}$ (for definition of the orbitals see Figure 5).

$$
\psi=0.977 a_{1}{ }^{2}-0.141 b_{1}^{2}-0.162 b_{2}{ }^{2}
$$

Thus, the higher configurations account for $4.6 \%$ of the wavefunction, indicating a nearly pure closed-shell state. This result


Figure 7. Contribution of higher configurations to the wavefunction of the cyclobutne dication system as a function of the reaction coordinate $r$. The CI eigenvector was calculated with a MNDO full CI calculation and imposed $D_{2 h}$ symmetry.
has been confirmed by a MC-SCF optimization of 11 with a $3-21 \mathrm{G}$ basis set. According to the MNDO CI eigenvector, a proper choice of the valence space should include the $a_{1}, b_{1}$, and $b_{2}$ orbitals (HOMO, LUMO, and LUMO+1, Figure 5). A three-configuration MC-SCF optimization using this valence space with a standard $3-21 \mathrm{G}$ basis and imposed $D_{2 h}$ symmetry predicts the coefficients of the higher configurations $b_{2}{ }^{2}$ and $b_{1}{ }^{2}$ to be 0.2044 and 0.1364 , i.e., a contribution of $6 \%$ to the wavefunction. For an idealized diradical, like the two ethylene radical cations at an infinite distance, this contribution would be exactly $50 \%$ (Figure 7), whereas the "normal" closed-shell 1,4-butadiyl dication 8 shows $1.7 \%$ contribution of higher states. Thus, singlet-triplet, MC-SCF, and CI calculations all predict a quite pure closed-shell state for 11. The diradicaloid character should increase both on shortening and on lengthening the distance between the two formal ethylene radical cation units.

In view of the critical importance of the distance $r$ in controlling chemical and physical properties of cyclobutane dication systems (Figures 6 and 7), a reliable estimate for this parameter is needed to determine the electronic structure of the pagodane dication. The results of semiempirical calculations have to be regarded with caution, since these methods have not been parameterized to treat such extraordinary structures. The $3-21 \mathrm{G}$-optimized structure of 11 agrees quite reasonably with the MC-SCF-optimized geometry ( $r$ is predicted $0.07 \AA$ too short, all other bond lenghts agree within $0.01 \AA$ ). Because of technical computer and program limitations, the pagodane dication was optimized with a standard 3-2IG basis set. The critical distance $r$ in the pagodane was found to be $2.165 \AA$ (Table III), i.e., considerably shorter than the MNDO value ( $2.592 \AA$ ). Even if this distance is ca. $0.07 \AA$ too short, there should be much better overlap between the two formal ethylene radical cation units compared to that expected from the MNDO calculation. According to our CI calculations (Figures 6 and 7), this value lies within the range of lowest diradical character and optimum stability.
Since the electronic structure should strongly depend on this separation parameter $r$, we have examined various conceivable structures (Figure 8).
The dications 13, 14, 15, and 4 have been optimized with a standard $3-21 \mathrm{G}$ basis set. With $r=1.974 \AA$, the norbornadiene dication 13 (Figure 8) does have a distance $r$ somewhat shorter than the optimum value, but still within the "closed-shell range". A harmonic vibration frequency analysis at the 3-21G level predicts it to be a minimum on the potential energy hypersurface. Indeed, the hexamethyl derivative 7 has been synthesized by Hogeveen et al. via ionization and rearrangement of a tricyclic alcohol. ${ }^{3}$

Structure 14, whose potential precursor (the corresponding diene) is known, ${ }^{18}$ also exhibits a favorable distance $r$ (Figure 8 ).

[^6]

13


15

14



Figure 8. Cyclobutane dication systems with different frameworks and values of the "critical distance" $r$. Geometries were calculated with a standard $3-21 \mathrm{G}$ basis set. 13 and 15 were confirmed to be minima by harmonic frequency analysis. 14 is a transition state.

A frequency analysis, however, predicts one imaginary frequency (analogous to mode a in the parent dication). According to further optimization with lower symmetry constraints, 14 turns out to be the transition state of the automerization reaction of a rhomboid structure with $C_{2 h}$ symmetry 15 and the two positive charges largely localized at the bridgehead carbons. Experimentally, this tendency is manifested in cross-transannular bonding upon electrophilic attack. Structure 15 was confirmed to be an energy minimum by harmonic frequency analysis. At the 3-21G level, it is $8.6 \mathrm{kcal} / \mathrm{mol}$ more stable than $D_{2 h} 14$. Upon consideration of correlation energy (MP2/3-21G//3-21G), this value is reduced to $1.8 \mathrm{kcal} / \mathrm{mol}$. The cationic system corresponds to the parent rhomboid structure 9 proposed by Hoffmann. ${ }^{4}$ Obviously, this system is not as rigid as the norbornane or pagodane framework; it lacks a "cross-bracing" to prevent the system from rhomboid distortion. This "cross-bar" is formed by the $\mathrm{CH}_{2}$ bridge in 13 and the $\mathrm{C}-\mathrm{C}$ bond centrally above the four-membered ring in 4.

Analogous to [1.1.1.1]pagodane, the [1.1.2.2]pagodane when treated in $\mathrm{SO}_{2} \mathrm{ClF}$ solution with $\mathrm{SbF}_{5}$ at $-80^{\circ} \mathrm{C}$ is oxidized to give the corresponding dication $16 .{ }^{2,19}$


16
This cationic species is considerably less stable than the [1.1.1.1] derivative. Even at $-20^{\circ} \mathrm{C}$, rearrangement to a bisallylic dication occurs. The instability can be rationalized in terms of larger diradical character. Due to larger bridge sizes (ethylene instead of methylene moieties), the distance $r$, and thus the extent of the diradical character, increases. Side reactions yielding closed-shell cations thus become more probable.

In contrast, the dodecahedrane dication 17 mentioned recently by Prinzbach et al. ${ }^{20}$ does not have a chance to profit from aro-

[^7]Table IV. Experimental and iglo Calculated ${ }^{13} \mathrm{C}$ Chemical Shifts of 4 and $5^{a}$

5 rapid equilibrium of classical structures $C_{2}$

|  | 4 |  |  |  | 5 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3-21G |  | MNDO |  | MNDO |  | $\operatorname{expt}_{\delta}^{1,2}$ |
|  | $\delta^{a}$ | $\Delta \delta$ | $\delta$ | $\Delta \delta$ | $\delta$ | $\Delta \delta$ |  |
| a | 241.6 | -9.4 | 261.2 | 10.2 | $(417.5+101.8) / 2=259.6$ | 8.6 | 251.0 |
| b | 49.0 | -8.2 | 50.8 | -6.4 | $(64.4+46.9) / 2=55.6$ | -1.5 | 57.2 |
| c | 47.2 | -5.1 | 49.4 | -2.9 | $(48.4+57.5) / 2=53.0$ | 0.7 | 52.3 |
| d | 53.9 | -11.4 | 64.9 | -1.1 | 45.5 | -19.3 | 65.3 |

${ }^{2}$ Input geometries are optimized with MNDO and 3-21G. 1GLO chemical shifts are calculated with a DZ basis (basis I). ${ }^{b}$ Values in parts per million relative to TMS.
matic stabilization since the two ethylene radical cation units are separated by a distance of more than $3 \AA$.


17
Whereas the [1.1.1.1] and [1.1.2.2]pagodane dications are stable in solution, the dications of the corresponding "half-pagodanes" could only be generated in the gas phase by charge-stripping experiments. ${ }^{15}$

## ${ }^{13} \mathrm{C}$-Shift Calculations

IGLO ${ }^{13} \mathrm{C}$-shift calculations ${ }^{14}$ have proven to be a powerful tool in structural carbocation chemistry. ${ }^{21}$ Comparison of experimental and calculated ${ }^{13} \mathrm{C}$ chemical shift values should provide further evidence in discriminating the structural hypotheses 4-6. MNDO geometries of the aromatic $D_{2 h} 4$ and the classical 5 as well as the ab initio $3-21 \mathrm{G}$ geometry of 4 were used for IGLO calculations performed with DZ basis set (Table IV).

Even though there is indication for a $\sigma$-aromatic system, the results cannot be interpreted unambiguously in favor of 4 . For both structures, the nonclassical 4 and the classical 5, rather low-field shifts of the cationic centers a are predicted. The iglo calculated shift of carbon atoms a in 4 based on the MNDO geometry is 10 ppm low field and the value based on the 3-21G geometry 10 ppm high field compared to the experimental value. Obviously, the predicted chemical shifts are a sensitive function of the geometry. ${ }^{22}$ Most surprising are the predicted chemical shifts for the cationic centers in the "open" structure 5 . With $\delta$ 259 the average shift $\left(a+a^{\prime}\right) / 2$ is predicted to be within the same range as in the nonclassical compound 4. The same is true for the nuclei c . In 4 , these carbon atoms are centrally located above the $2 \pi$-plane and should be shielded if the ring current were

[^8]

Figure 9. HOMO of the pagodane dication. Coefficients are calculated with MNDO and plotted with PERGRA. ${ }^{23}$
present. The change in chemical shift in going from pagodane ( $\delta 59.6$ ) to 4 ( $\delta 52.3$ ) is in the expected direction, although the change is small. Our IGLO calculations agree, but a similar upfield shift is predicted for the classical structure 5 (calculated $\delta 53.01$, observed $\delta 52.3$ ). The upfield shift has been interpreted in terms of a ring current in $4 .^{2}$ On the basis of the IGLO results, however, this does not exclude a classical structure. Obviously, in the field of dications shielding and deshielding effects have to be interpreted very carefully. They cannot unequivocally be interpreted to be due to a ring current or any aromaticity effect, as this is usually the case with neutral compounds.

In contrast to $c$, the nuclei $d$ should be located within the deshielding range of the ring current. Fortunately, in this case the interpretation is less ambiguous. Iglo predicts a downfield shift for the aromatic structure $4(\Delta \delta=12 \mathrm{ppm}, 3 / 21 \mathrm{G}, \Delta \delta=$ $22.4 \mathrm{ppm}, \mathrm{MNDO}$ ) compared to the neutral pagodane 1 and an almost constant value for the nonclassical ion $5(\Delta \delta=3.6 \mathrm{ppm})$. The experimental value ( $\Delta \delta=23.4 \mathrm{ppm}$ ) clearly favors a nonclassical structure.

## Aromaticity of Cyclobutane Dicationic Systems

There is an inherent difficulty in answering the question whether a given compound is aromatic or not. In contrast to energy and geometry, aromaticity is not a quantum theoretical observable (operator acting on a wavefunction leading to an expectation value) and thus not a yes or no question. Usually, the term aromatic is justified by the examination of observables like bond alternation (geometry), stabilization versus any reference (energy), nuclear magnetic resonance, etc. Since the electronic structure (aromaticity) of the pagodane dication is a consequence of its $D_{2 h}$ symmetry, we first determined the structure. According to our calculations, there is little doubt that the pagodane dication has $D_{2 h}$ symmetry since we disproved the two alternatives ( $C_{2 v}$ equilibrium 5 and diradical structure 6), which also comply with the experimental data.

After having elucidated the geometry, we turn to the question of if the electronic structure of the pagodane dication should be termed aromatic. We have reasons for an affirmative answer.

The two-electron delocalized system in the pagodane dication is built up by a set of four MO's, which are equivalent to those of the model compound the rectangular cyclobutane dication 11 (Figure 1). As shown in Figure 9 for the HOMO of pagodane dication, the coefficients at other carbon atoms in the pagodane framework are low (<0.1).

Thus, there is no significant conjugative effect of orbitals of the pagodane framework disturbing the topology of the four cyclobutane orbitals. The four MO's describing the four-center two-electron delocalized system are separable from those describing the molecular frame in a first-order approximation. The pagodane framework merely holds the delocalized system together and can thus be compared with the $\sigma$-frame in benzene and related aromatic systems. ${ }^{24}$

Since the sets of MO's for both the cyclobutane and cyclobutadiene dication are topologically equivalent, all arguments for

[^9]

Figure 10. Natural bond orders in the HOMO's of rectangular cyclobutane dication ( $D_{2 k}$ ) and square cyclobutadiene dication ( $D_{4 k}$ ), calculated with $6-3.1 G^{*} / / / 6-31 \mathrm{G}^{*}$.
aromaticity in the cyclobutadiene dication should also be qualitatively valid for cyclobutane dication and hence for pagodane dication and related systems. This analogy is still valid on a quantitative level. The interaction of the porbitals building up the delocalized system can be rationalized by analyzing their contribution to the overall bond orders. There are two different modes of overlap involved in the cyclobutane dication system. One is of $\pi$-character along the shorter side of the rectangle and the other is $\sigma$ on the longer side. According to a natural bond order analysis, ${ }^{25}$ both interactions are almost equivalent even though the bond lengths differ strongly (Figure 10 ).

Orbital overlap of two carbon p orbitals separated by a distance of $1.43 \AA$ in a $\pi$-bond is of the same order ( 0.23 ) as a $\sigma$-overlap with a bond distance of $2.11 \AA(0.21){ }^{26} \quad$ Both bond orders compare well with the $\pi$-bond orders in the square cyclobutadiene dication, and both orbitals are of similar energy ( -0.9 eV in cyclobutane and -0.89 eV in cyclobutadiene dication). Thus, any stabilization arising from delocalization of the two electrons should be roughly of the same magnitude in both systems.
Following the original definition of $\sigma$ - and $\pi$-bonds, which defines orbitals lying in the plane of a planar $\pi$-system as $\sigma$ and those perpendicular to the plane as $\pi$, the pagodane dication and related systems contain perfectly $\sigma$-delocalized systems with two electrons. A similar $\sigma$-delocalization was discussed by Dewar ${ }^{27-29}$ and Cremer ${ }^{30,31}$ for cyclopropane. Most of the unusual properties of cyclopropane are convincingly explained assuming a $\sigma$-aromaticity, even though Cremer ${ }^{31}$ criticized the term $\sigma$-aromaticity since "it applies essentially to one class of compounds, namely the cyclopropanes." Rectangular cyclobutane dications could now be viewed as a second class.

Delocalization in rectangular cyclobutane dication systems, however, can be clearly distinguished from the concept of $\sigma$ conjugation introduced by Dewar and Petit, ${ }^{32}$ which is based on the fact that resonance integrals between different hybrid AOs of a given atom do not vanish even if the AOs are orthogonal. In rectangular cyclobutane dication 11 as well as in the pagodane dications 4 and 16, the AOs involved in the delocalized system are almost pure p orbitals (Figure 9).
Separability of the delocalized system (Figure 9), cyclic delocalization (Figure 10), $4 n+2$ electrons, together with ${ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}$ NMR data, ${ }^{2}$ and cyclovoltammetry of $4^{33}$ justify the term aromatic. Even though a stabilization cannot be expressed quantitatively because the choice of the reference compound is arbitrary, stabilization should be of the same order as in the cyclobutadiene dication.

[^10]
## Conclusion

For a rectangular, $\sigma$-aromatic cyclobutane dication, like the pagodane or the norbornadiene dication, to be stable, some prerequisites are essential:
(1) A rigid molecular framework is needed to prevent in-plane distortion toward the rhomboid form or out of plane motion toward $D_{2 d}$ symmetry (imaginary vibrational frequency modes of the parent compound 11, Figure 4).
(2) The two formal ethylene radical cation units have to be held at distances between $\sim 1.9$ and $2.3 \AA$ to keep the diradicaloid character low enough to prevent side reactions.

Another conclusion can be drawn from the numerous experiments aimed at oxidizing cyclobutane containing compounds: the cyclobutane system has to be octasubstituted, perhaps due to both kinetic and thermodynamic stabilization. ${ }^{34}$

The pagodane dication and the norbornadienyl dication can be viewed as frozen aromatic transition states of the reaction of two ethylene radical cations in the sense of the Dewar/Evans principle. ${ }^{16}$ A cycloaddition of two neutral ethylene molecules in $D_{2 h}$ symmetry is forbidden because the transition state would be antiaromatic (triplet diradical), while the product cyclobutane again is closed shell. Removing two electrons from the system reverses the picture. The educts are two ethylene radical cations, the transition state is aromatic (almost pure closed shell), and the product, the square cyclobutane dication, again is diradical. The formal transition state now is a minimum on the reaction path within $D_{2 h}$ symmetry because of its aromatic stabilization. This stabilization, however, has to be paid for by a strong Coulomb repulsion of the two positive charges. If the system is not constrained within a $D_{2 h}$ symmetry by a rigid molecular framework, the charges will be separated by distortion toward a rhomboid or tetrahedral geometry and bishomoaromaticity will be canceled. Hence, it should be possible to synthesize molecules corresponding to some other points on the reaction coordinate and thus test the limits of homoaromaticity.

The rectangular cyclobutane dication is also interesting from another point of view. It is the third in a set of topologically
(34) Norbornadiene or quadricyclane cannot be oxidized to form the corresponding dication. Reaction with $\mathrm{SbF}_{5}$ in $\mathrm{SO}_{2} \mathrm{ClF}$ even at very low temperatures occurs violently to form black polymers. Herges, R.; Prakash, G. K. Unpublished results. For other unsuccessful attempts to oxidize cubane, homocubane, bishomocubane, and related, not fully substituted cyclobutane systems, see: ref $2, \mathrm{p} 7767$.
different two-electron four-center hydrocarbon aromatic compounds, which have been verified experimentally.


$\mathrm{D}_{4 \mathrm{~h}}$

$T_{d}$

None of these ideal arrangements is an energy minimum without extra stabilization by substitution. The square $D_{4 h}$ cyclobutadiene dication is a transition state for the ring inversion of the puckered structure. ${ }^{21 a, 35}$ The tetrahedral dication needs six $\mathrm{CH}_{2}$ bridges on all edges of the tetrahedron (realized in the adamantane framework) ${ }^{21 b}$ to be a relative minimum on the energy hypersurface. Their instability notwithstanding, such dications can serve as models illustrating the concepts of aromaticity and isolobal structures.

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Registry No. 4, 99828-64-5; 15, 132646-10-7; ethylene radical cation, 34470-02-5; 1,4-butanediylium, 111160-98-6; norbornadiene dication, 132832-60-1.

Supplementary Material Available: Full calculational details of ab initio calculations of $\mathbf{4}, 13,14$, and 15 ( 20 pages). Ordering information is given on any current masthead page.
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# Structures of $\mathrm{Ag}_{2} \mathrm{X}^{+}$and $\mathrm{Cu}_{2} \mathrm{X}^{+}$Ions: Comparison of Theoretical Predictions with Experimental Results from Mass Spectrometry/Mass Spectrometry 

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#### Abstract

Daughter ion MS/MS mass spectra have been recorded for $\mathrm{Ag}_{2} \mathrm{X}^{+}$and $\mathrm{Cu}_{2} \mathrm{X}^{+}$parent ions in which X is $\mathrm{H}, \mathrm{CH}_{3}$, $O$, or $C O$. Consideration of the dissociation processes observed suggests the prevalence of certain ion structures out of the several possible for these combinations of atoms. The suggested structures are compared with theoretical predictions based on Hartree-Fock SCF calculations using the relativistic ECP approximation. Present theoretical results agree with the rationalizations of the daughter ion $\mathrm{MS} / \mathrm{MS}$ experiment in the assignment of a linear structure to $\mathrm{Ag}_{2} \mathrm{H}^{+}, \mathrm{Ag}_{2} \mathrm{O}^{+}$, and $\mathrm{Cu}_{2} \mathrm{O}^{+}$. Theoretical predictions of linear $\mathrm{Ag}_{2} \mathrm{CH}_{3}{ }^{+}$and $\mathrm{Cu}_{2} \mathrm{CH}_{3}{ }^{+}$are also supported by experimental work with mass spectrometry/mass spectrometry. Bent geometries are predicted for $\mathrm{Ag}_{2} \mathrm{CO}^{+}$and $\mathrm{Cu}_{2} \mathrm{CO}^{+}$by the calculations performed.


## Introduction

Mass spectrometry/mass spectrometry (MS/MS) is a powerful tool for ion structure elucidation. ${ }^{1}$ To record a daughter ion

[^11]MS/MS spectrum, a parent ion of specified mass is selected from all ions formed in the source of the mass spectrometer, excited

[^12] Spectrometry: Techniques and Application of Tandem Mass Spectrometry, VCH Publishers: New York, 1988.


[^0]:    Dedicated to H. Prinzbach on the occasion of his 60 th birthday.
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